

Q: Why can you not give a fermion a vev?

A: Fermions transform in $\frac{1}{2}$ rep. of

Lorentz symmetry

$$\psi \rightarrow (\Lambda^\mu_\nu)^{1/2} \psi$$

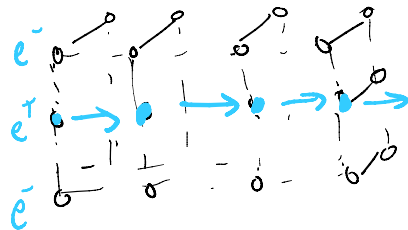
↳ spinor basis
to contract Lorentz indices

$$\langle \psi \rangle \rightarrow \underbrace{(\Lambda^\mu_\nu)^{1/2}}_{\text{constant}} \langle \psi \rangle$$

Q: Vectors getting vev?

A. $\langle A_\mu \rangle = \text{const.}$

Establishing a preferred frame.



Example of broken symmetry.

Crystal lattice structure does not respect continuous symmetry

Distinction is

$\angle$ is Lorentz invariant

↳ describes interactions of ions under QED

But expanding on background that breaks to Lorentz symmetry.

Scalar vevs do not break Lorentz:

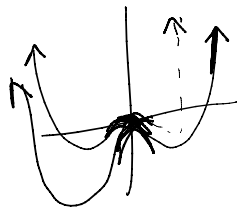
the vev background has no preferred direction, no preferred orientation

Q: At high T , Higgs potential in SM?

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A: True that @ high T , we expect Higgs potential to restore EW symmetry.

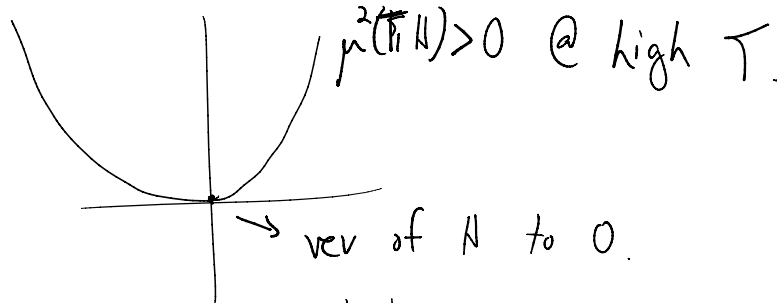
$$\text{At } T=0: V = \mu^2 |H|^2 + \lambda |H|^4, \quad \mu^2 < 0$$



$$\text{At high } T: V = \mu(T, H)^2 |H|^2 + \lambda(T, H) |H|^4$$

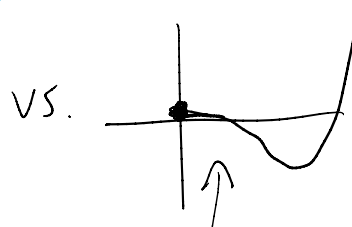
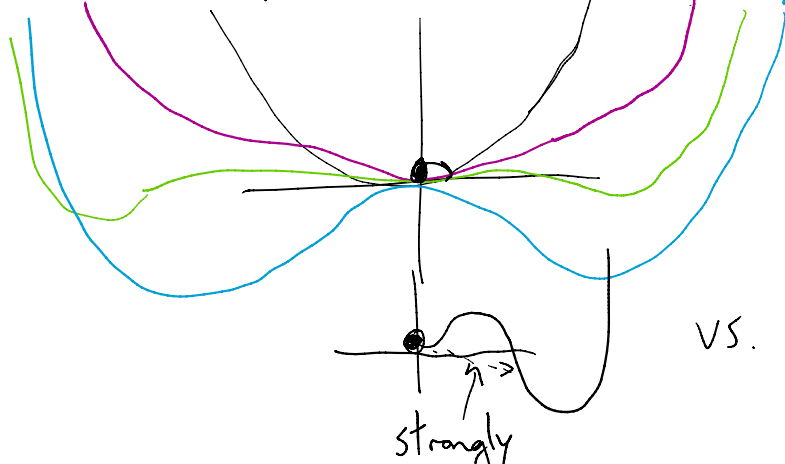
$\mu^2(0, H) \sim$ 1-loop, n -loop corrections to μ^2 field value

$\mu^2(T, H) \sim$ $T=0$ corrections +
finite T corrections independent of $\langle H \rangle$,
finite T corrections dependent on $\langle H \rangle$



$\mu^2(T, H) > 0$ @ high T .

Temperature cools: $T \downarrow$ high T_{int} T_{int} $T=0$



↑
strongly
first order
phase transition

↑
second order
phase transition

In SM, we calculate & find that
for SM masses & couplings, we expect
a second order phase transition.

What is this calculation? &

Why do we need a first order
phase transition for EW baryogenesis?

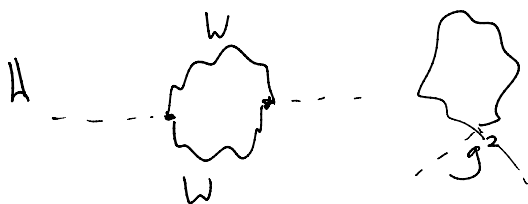
① Calculation

Evaluate Coleman-Weinberg 1-loop correction
to $V_{SM}(H)$, and include finite T effects.

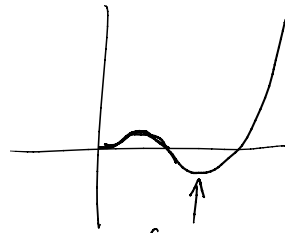


$$V_{\text{corr.}} \sim (-1)^{2s} \lambda^2 \log \left(\frac{H^2}{M^2} \right)$$

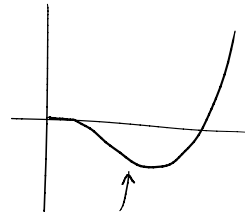
$$V_{\text{full}} = \mu^2 |H|^2 + \lambda |H|^4 + \sum_{f,b} (-1)^{2s} \lambda_{f,b}^2 \log \left(\frac{H^2}{M^2} \right)$$



↑
fermions
negative
bosons pos. (check signs)



fermion
contrib. stronger
to get 1st order



boson
contrib. overwhelms
fermions

If you do calc. with arbitrary
top mass, fix W , get SFOP
for $m_t < 60 \text{ GeV}$. Our $m_t = 173 \text{ GeV}$.

Or For $m_h < 42 \text{ GeV}$

A: Why SFOP necessary?

3 commonly cited conditions for baryogenesis

Sakharov:

① B violation

② C + CP violation

③ Out of thermal equilibrium process.

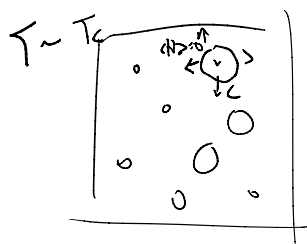
↳ In SM, B violation from EW sphalerons.

nonperturbative, weakly coupled tunneling amplitudes
that are very suppressed @ low T but unsuppressed
@ high T .

EW sphaleron process act during the phase transition
from $\langle H \rangle = 0$ to $\langle H \rangle = v$.

Only when tunneling amplitude between $\langle H \rangle = 0$ &
 $\langle H \rangle = v$.

Universe



$$\Rightarrow \Delta B = 0$$

bubble wall



$$\Delta B \neq 0$$

$$\Delta B \neq 0$$

$\rightarrow c$

For 2nd PT, too smooth, bubbles do not form.
no baryon asymmetry.